

SUBJECT CODE NO:- E-95
FACULTY OF ENGINEERING AND TECHNOLOGY
T.E.(CSE/IT) Examination Nov/Dec 2017
Theory of Computation
(REVISED)

[Time: Three Hours]

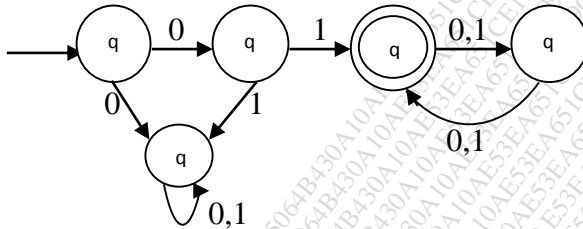
[Max.Marks:80]

Please check whether you have got the right question paper.

- N.B
- i. Q. No. 1 and Q.No.6 are compulsory.
 - ii. Attempt any two questions from Q.No.2 to Q.No.5 and two questions from Q.No.7 to Q.No.10 of each section.
 - iii. Figures to the right indicate full marks.

SECTION A

- Q.1 Attempt any five questions from the following : 10
- a) Determine whether the following DFA accepts the string 011101 or not.



- b) Define context-free grammar with suitable example.
- c) Differentiate between NFA and DFA.
- d) Find regular expression for set of all strings over {0, 1} ending with 11 and beginning with 100.
- e) State Arden's Theorem. Where is it required?
- f) Let $G = (\{S\}, \{a,b,t,*\}, P, S)$ where P consists of : $S \rightarrow S+S \mid S^*S \mid a \mid b$. Derive $a + a^*b$.
- g) Construct a finite automata for the regular expression $10(0+1)01$.
- h) Define Moore Machine with an example.

- Q.2 a) Construct DFA equivalent to given NFA: 08
- $(\{p, q, r, s, t\}, \{0,1\}, \delta, p, \{s\})$
 Where δ is given by

States/ Σ	0	1
$\rightarrow p$	{p, t}	{p, q}
q	\emptyset	{r}
r	{r}	{r}
*s	{s}	{s}
t	{s}	\emptyset

- b) Define ambiguity in CFG. Show that the following CFG is ambiguous: 07
- $S \rightarrow aB \mid aA, A \rightarrow aAB \mid a \mid b, B \rightarrow Abb \mid b$.

- Q.3 a) Describe the closure properties of regular languages. 07
 b) Construct a Moore machine equivalent to following Mealy machine: 08

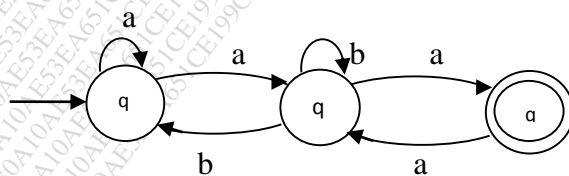
Present State	Next state			
	a=0	Output	a=1	Output
→ q ₁	q ₁	1	q ₂	0
q ₂	q ₄	1	q ₄	1
q ₃	q ₂	1	q ₃	1
q ₄	q ₃	0	q ₁	1

- Q.4 a) Show that $L = \{a^p \mid p \text{ is a prime}\}$ is not regular language. 07
 b) Let $G = S \rightarrow 0B \mid 1A, A \rightarrow 0 \mid 0S \mid 1AA, B \rightarrow 1 \mid 1S \mid 0BB$, for string 11001010, 08
 Find: i) leftmost derivation,
 ii) rightmost derivation,
 iii) parse tree

- Q.5 a) Draw finite automata for the following transition table & construct minimum state automata equivalent to it: 08

States/ Σ	0	1
→ A	B	C
B	D	E
C	F	G
(A)	D	E
E	F	G
(F)	D	E
(G)	F	G

- b) Consider the following finite automata prove that the strings recognized are:- 07
 $(a + a(b + aa)^*b)^* a(b + aa)^*a$

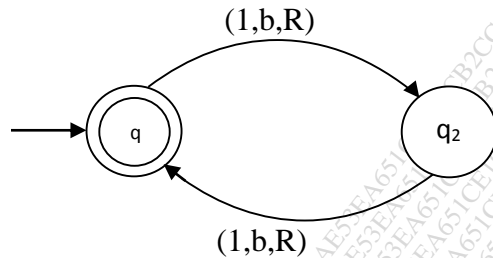


SECTION B

Q.6 Attempt any five question from the following:

10

- a) Construct PDA for the following CFG:
 $s \rightarrow a | aS | bSS | SSb | SbS$.
- b) Define Chomsky Normal form with suitable example.
- c) Differentiate between recursive & recursively enumerable languages.
- d) Determine whether the string 1111 is accepted by the following Turing machine.



- e) Discuss halting problem in Turing machine.
- f) Define deterministic pushdown automata formally.
- g) Explain decision problems involving context-free languages.
- h) Let G be $S \rightarrow AB$, $A \rightarrow a$, $B \rightarrow C|b$, $C \rightarrow D$, $D \rightarrow E$ & $E \rightarrow a$. Eliminate unit productions and get equivalent grammar.

Q.7 a) Find reduced grammar equivalent to G whose productions are:

07

$S \rightarrow AB|CA$, $B \rightarrow BC|AB$, $A \rightarrow a$, $C \rightarrow aB|b$.

b) Construct a grammar in Greibach normal form equivalent to the grammar.

08

$S \rightarrow AA|a$, $A \rightarrow SS|b$.

Q.8 a) Construct a PDA for the language $L = \{ ww^R \mid w \in \{a,b\}^* \}$ where w^R is reverse of w

08

b) Explain various programming techniques for Turing machine with suitable example.

07

Q.9 a) Design a TM over $\{1, b\}$ which can compute a concatenation function over $\Sigma=\{1\}$. 07

b) Construct a CFG 'G' which accepts $N(A)$, where, $A=(\{q_0, q_1\}, \{a, b\}, \{z, z_0\}, \delta, q_0, z_0, \emptyset)$ and δ is given by-

- $\delta(q_0, b, z_0) = \{(q_0, zz_0)\}$
- $\delta(q_0, \Lambda, z_0) = \{(q_0, \Lambda)\}$
- $\delta(q_0, b, z) = \{(q_0, zz)\}$
- $\delta(q_0, a, z) = \{(q_1, z)\}$
- $\delta(q_1, b, z) = \{(q_1, \Lambda)\}$
- $\delta(q_1, a, z_0) = \{(q_0, z_0)\}$

Q.10 a) Explain the model of linear bounded automata in detail. 07

b) Find a grammar in CNF equivalent to the following grammar:
 $S \rightarrow aAbB, A \rightarrow aA \mid a, B \rightarrow bB \mid b$ 08